

Proceedings Article

# Domain-weighted Block Coordinate Descent for Quantitative Single-sided MPI Reconstruction

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## Abstract

Single-sided Magnetic Particle Imaging (MPI) provides a solution suitable for intraoperative localization. However, asymmetric coil arrangements cause nonuniform magnetic fields and depth-dependent sensitivity decay, leading to biased reconstructions. This paper proposes a domain-weighted Block Coordinate Descent (DW-BCD) algorithm for quantitative single-sided MPI reconstruction. A preliminary reconstruction estimates the signal support domain, from which weighting and regional partitioning are derived. The subsequent reconstruction combines block-wise domain-weighted  $l_1$  and global total variation(TV) regularization. Experiments show that DW-BCD effectively reduces depth-related concentration bias, enabling accurate quantitative reconstruction of magnetic nanoparticle distributions for clinical applications of single-sided MPI.

## I. Introduction

In system matrix-based Magnetic Particle Imaging (MPI), reconstruction can be formulated as an inverse problem [1]:

$$S \cdot c = u \quad (1)$$

where  $S \in X^{m \times n}$  is system matrix,  $c \in \mathbb{R}^n$  is the concentration distribution of magnetic nanoparticles (MNPs),  $u \in \mathbb{R}^m$  is the measured signal.

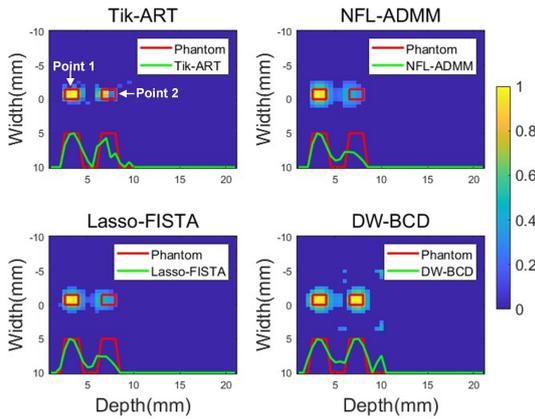
Conventional MPI systems adopt a closed configuration to generate uniform magnetic fields, enabling homogeneous sensitivity and accurate quantification [2]. However, their bulky structure limits portability. Single-sided MPI systems address this limitation by placing all coils on one side, allowing flexible detection and real-time op-

eration. Nevertheless, the asymmetric coil arrangement leads to depth-dependent field decay and variation in system-matrix column norms, causing commonly used reconstruction algorithms to yield biased particle concentration estimates at different depths.

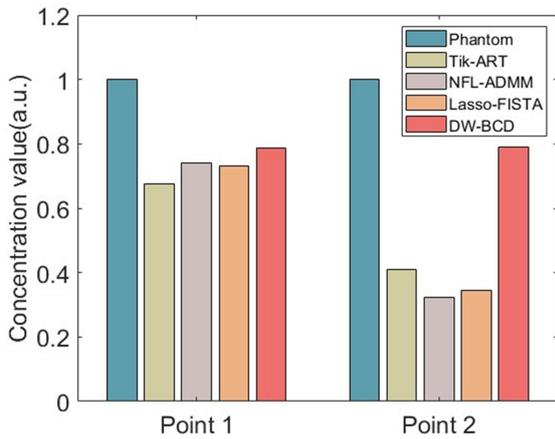
To this end, this paper proposes a reconstruction algorithm based on domain-weighted block coordinate descent for single-sided MPI to accurately quantify particle concentration distribution.

## II. Methods

The proposed domain-weighted block coordinate descent (DW-BCD) algorithm for single-sided MPI first performs a Landweber pre-reconstruction to estimate



**Figure 1:** Comparison of quantitative reconstruction performance of different reconstruction methods.



**Figure 2:** Comparison of mean intensity at different depths using different reconstruction methods

the MNPs distribution, from which the weighting mask  $W = [W_1, W_2, \dots, W_B]$  and block partitioning  $c = [c_1^T, c_2^T, \dots, c_B^T]^T$  (with  $B$  blocks) are derived. The reconstruction problem is further formulated as:

$$\min_{c \geq 0} \frac{1}{2} \|Sc - u\|_2^2 + \lambda_1 \|W \odot c\|_1 + \lambda_2 TV(c) \quad (2)$$

Where  $\|\cdot\|_2^2$  denotes the Euclidean norm,  $\|\cdot\|_1$  denotes the  $l_1$  regularization,  $\odot$  represents the Hadamard product,  $TV(\cdot)$  denotes the Total variational regularization,  $\lambda_1$  and  $\lambda_2$  are the regularization parameters.

According to the block partition obtained from the pre-reconstruction, the corresponding system matrix is denoted as  $S = [S_1, S_2, \dots, S_B]$ . The overall objective function is further decomposed into two subproblems for iterative optimization.

The first subproblem corresponds to the within-block optimization, formulated as:

$$c_b^{(k+1)} = \arg \min_{c_b \geq 0} \frac{1}{2} \|r_b^{(k)} - S_b c_b\|_2^2 + \lambda_1 \|W_b \odot c_b\|_1 \quad (3)$$

The residual  $r_b^{(k)}$  is determined based on the current estimates of all other blocks. In each iteration, all other blocks remain unchanged while the current block is updated independently.

The second subproblem involves a global TV regularization constraint across blocks:

$$c^* = \min_{c \geq 0} \frac{1}{2} \|c - \tilde{c}\|_2^2 + \lambda_2 TV(c) \quad (4)$$

where  $\tilde{c}$  is an intermediate solution obtained from the block-wise updates  $\tilde{c} = [c_1^{(k+1)}; \dots; c_B^{(k+1)}]$ .

### III. Results and discussion

Signals of two point-like phantoms at different depths were generated using the simulation framework established in our previous work [3], and were separated by 2 mm. The phantom locations are indicated by red boxes in Figure 1.

Three commonly used reconstruction methods (Tik-ART, NFL-ADMM, Lasso-FISTA) were evaluated. Compared with the shallow phantom (Point 1, Figure 1), all three underestimated the deeper phantom (Point 2), while DW-BCD maintained consistent intensities. Quantitative analysis of mean region intensities (Figure 2) confirms that conventional methods exhibit depth-dependent bias, which is absent in DW-BCD.

### IV. Conclusion

The DW-BCD-based method provides a feasible complement to the current SM-based single-sided reconstruction algorithms. It can effectively overcome the bias in estimating particle concentrations at different depths commonly observed in single-sided MPI reconstructions, thereby enhancing the quantitative reconstruction performance of single-sided MPI.

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### Author's statement

Conflict of interest: Authors state no conflict of interest.

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